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B. Sadigh, T. Lenosky, T. Oppelstrup, R. Minich,
G. Gilmer

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Shock-induced α - ω structural phase transformation of titanium: A molecular-dynamics study

Babak Sadigh, Thomas Lenosky,
Tomas Oppelstrup, Roger Minich,
and George Gilmer

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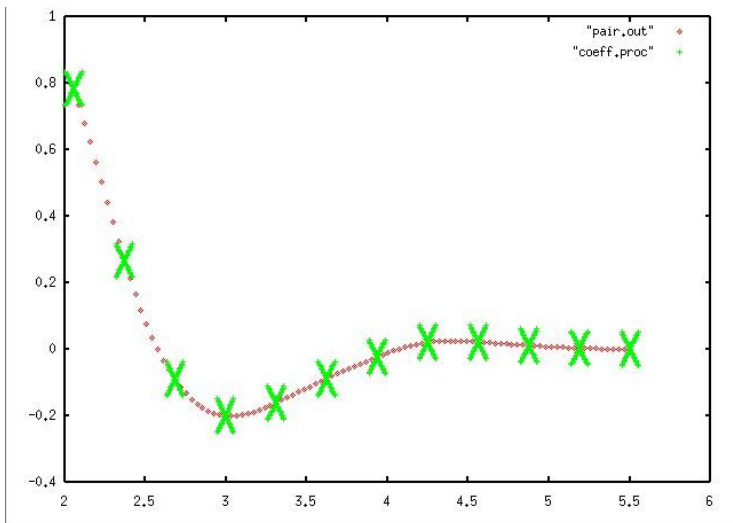
Outline

- Introduction – interatomic potentials, MEAM
- **Ti** – phase transformation
- Molecular-dynamics simulations of the shock-induced phase transformation of Ti.

MEAM Model Form

$$E_{tot} = \sum_{ij} \phi(r_{ij}) + \sum_i U(x_i)$$

$$x_i = \sum_j \rho(r_{ij}) + \sum_{jk} f(r_{ij}) f(r_{ik}) g(\cos(\theta_{jik}))$$



The various terms are represented by splines with many degrees of freedom, allowing much greater accuracy.

Two and three-body terms are summed over nearby atoms

Fitting Database

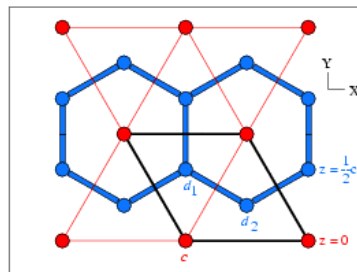
- **Energies**
 - for different crystal phases $E(V)$
 - Vacancy/Interstitial energies
 - Surfaces, clusters, other energies
- **Forces** – force matching method of Ercolessi and Adams
 - snapshots from MD
 - crystal with random displacements
- **Elastic constants and phonons**

Titanium Phases

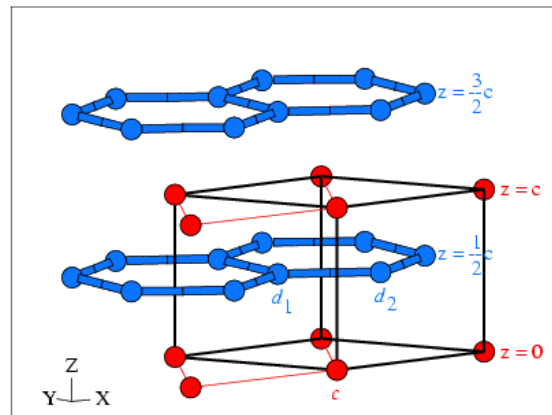
We want a model that describes α - ω Transitions

- Pathways for phase transformation
- Kinetics of moving interface, shock physics
- Atomic structure of moving interface

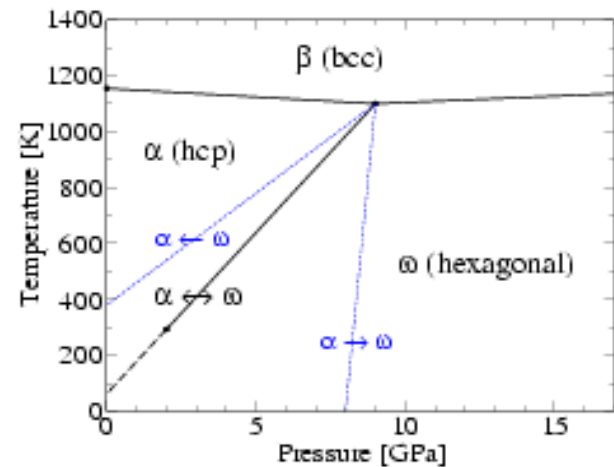
Hexagonal ($P6/mmm$) cell with 3 atoms
Prototype: MgB_2 structure



omega viewed along c axis



omega with exaggerated c axis (side view)

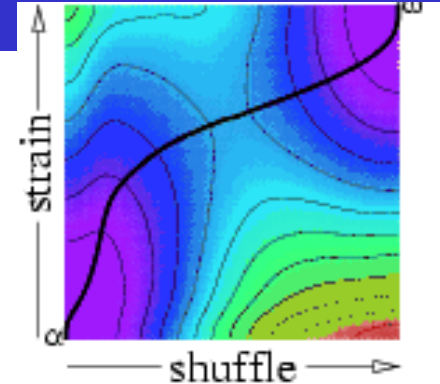


α is hcp (sphere packing)
but ω is a more complex phase

Ti Phase Transformation Barriers

D. R. Trinkle et al, Phys Rev Lett 91(2)
025701-1 (2003)

In this study pathways were systematically enumerated for Ti.



Each pathway consists of *shuffle* (atomic displacements within cell) and *strain* (changing shape of cell). Both are linearly interpolated.

Landscape barrier: Barrier in 2-D shuffle/strain plot

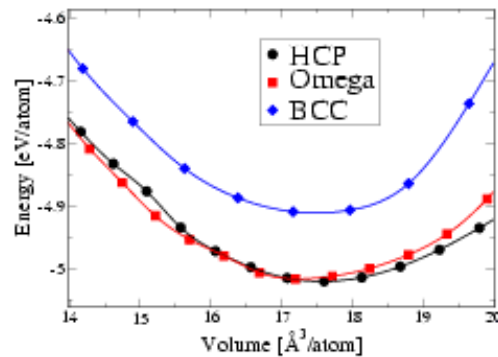
Actual barriers can then be found by relaxing atoms along path.

We want MEAM to predict correct barriers, landscape barriers used as test.

MEAM Potential for Titanium

- Classical model (Modified embedded-atom) of form used by T. Lenosky, et al.
- Parameterized to fit VASP crystal data, surface energies, and defect energies and forces

• Total Energy

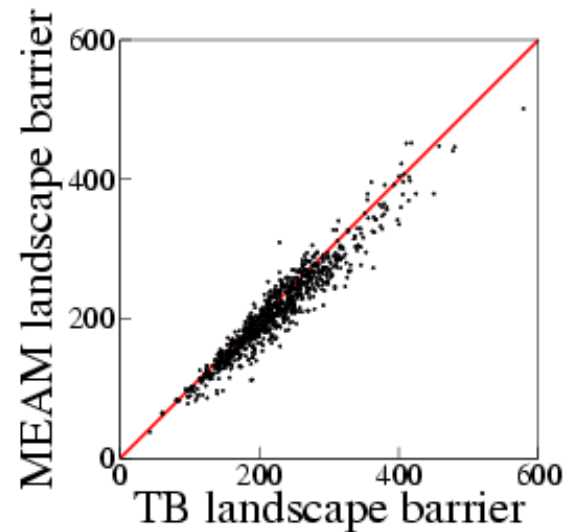


• Lattice Constants

| | <u>a</u> (Å) | <u>c</u> (Å) | <u>E</u> (eV) | <u>MEAM</u> <u>C₁₁</u> | <u>C₁₂</u> | <u>C₁₃</u> | <u>C₃₃</u> | <u>C₄₄</u> |
|------------|--------------|--------------|---------------|--------------------------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| hcp | 2.95 | 4.68 | -5.019 | 183 | 94 | 72 | 191 | 50 |
| omega | 4.58 | 2.82 | -5.015 | 197 | 87 | 56 | 234 | 35 |
| bcc | 3.27 | — | -4.910 | 96 | 108 | — | — | 39 |
| <u>GGA</u> | | | | | | | | |
| hcp | 2.95 | 4.67 | -5.171 | 176 | 87 | 68 | 191 | 51 |
| omega | 4.59 | 2.84 | -5.176 | 194 | 81 | 54 | 245 | 54 |
| bcc | 3.26 | — | -5.063 | 95 | 110 | — | — | 41.7 |

• Defect Energies

| <u>Defect</u> | <u>MEAM</u> (eV) | <u>GGA</u> (eV) |
|---------------|---------------------------|-----------------|
| hcp | | |
| Octahedral | 2.242 | 2.58 |
| Tetrahedral | unstable to dumbbell-0001 | |
| Dumbbell-0001 | 2.346 | 2.87 |
| Vacancy | 1.557 | 2.03 |
| Divacancy-AB | 2.828 | 3.92 |
| omega | | |
| Octahedral | 2.482 | 3.76 |
| Tetrahedral | 3.084 | 3.50 |
| Vacancy-A | 1.720 | 2.92 |
| Vacancy-B | 0.111 | 1.57 |



SHOCK (I)

Piston Velocity

1.1 km/s

Elastic Shock Wave
Speed:

7.0 km/s

Transformation
Shock Wave Speed:

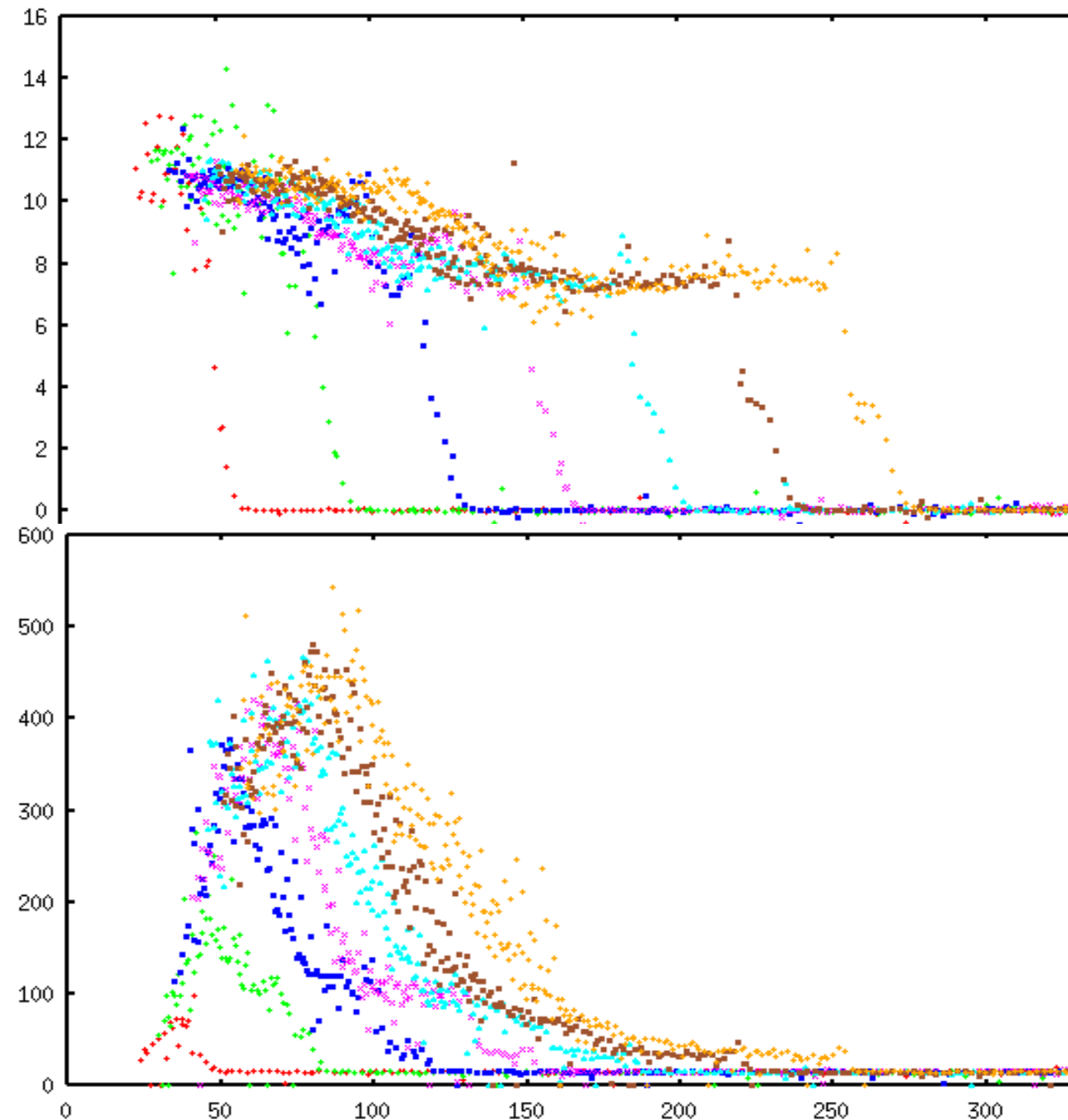
2.2 km/s

Shock Temperature:

450 K

Shock Pressure:

27 GPa



SHOCK (II)

Piston Velocity

1.5 km/s

Elastic Shock Wave
Speed:

7.0 km/s

Transformation
Shock Wave Speed:

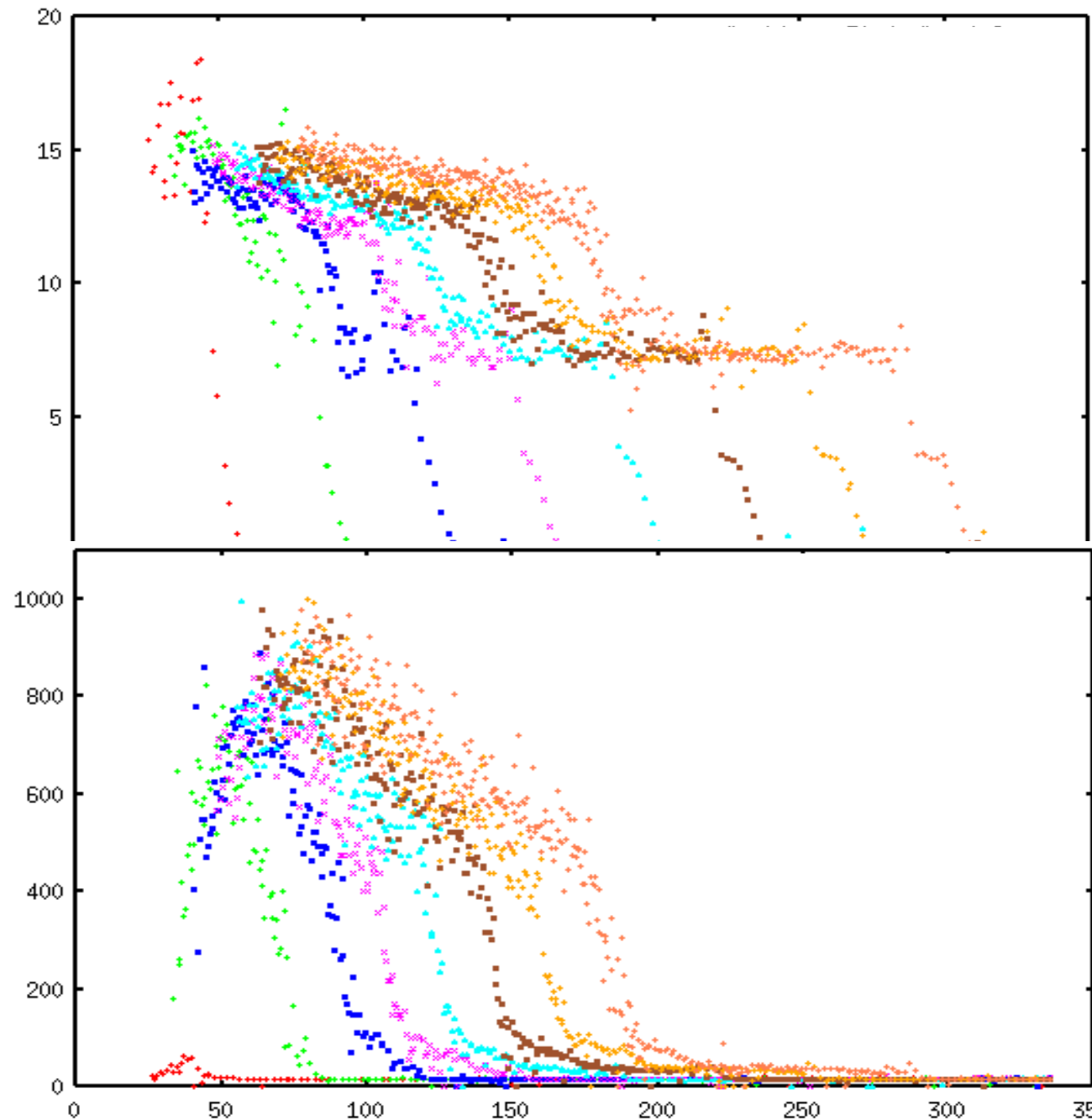
3.6 km/s

Shock Temperature:

900 K

Shock Pressure:

43 GPa



SHOCK (III)

Piston Velocity

2.0 km/s

Elastic Shock Wave
Speed:

7.0 km/s

Transformation
Shock Wave Speed:

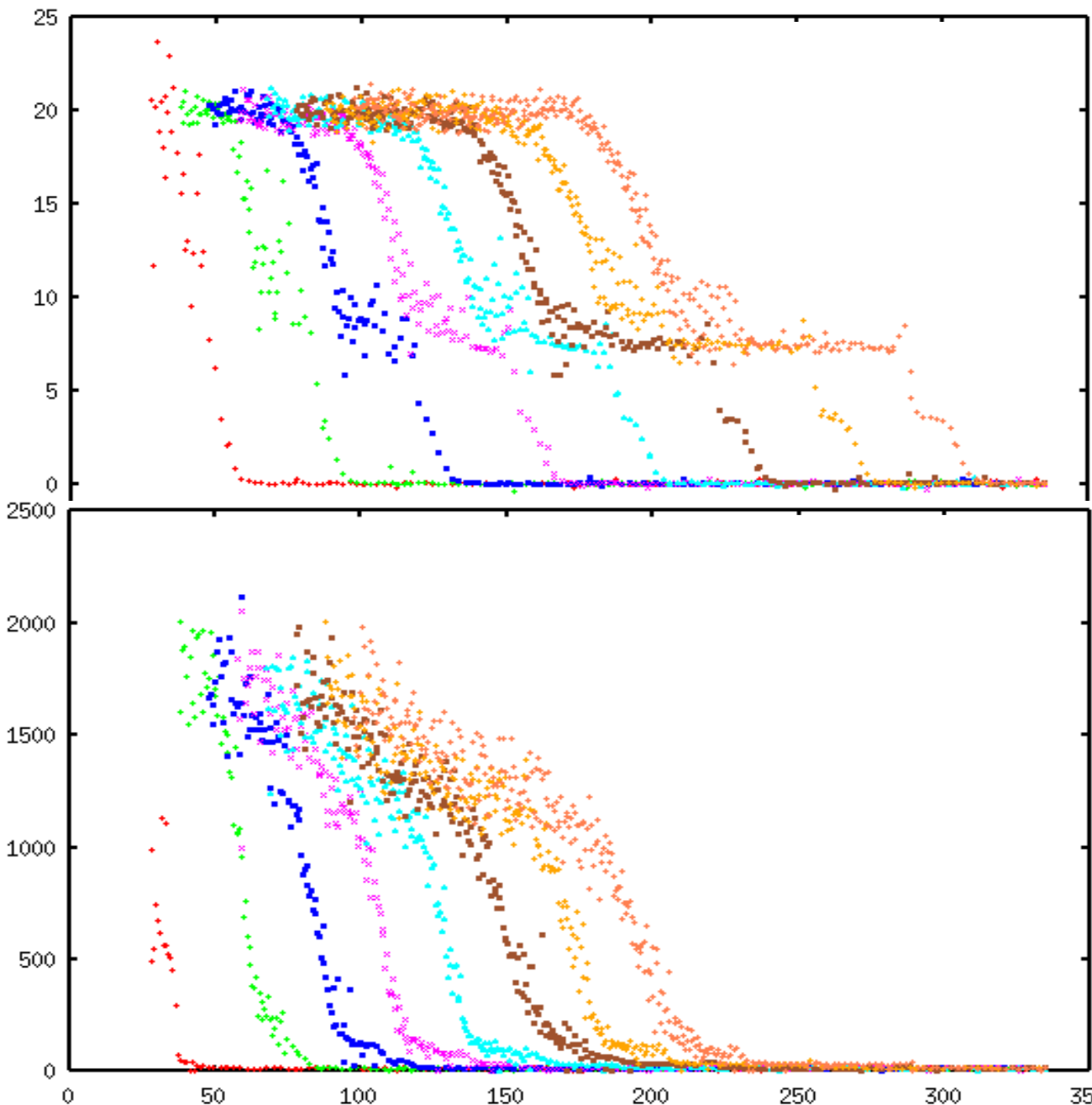
4.2 km/s

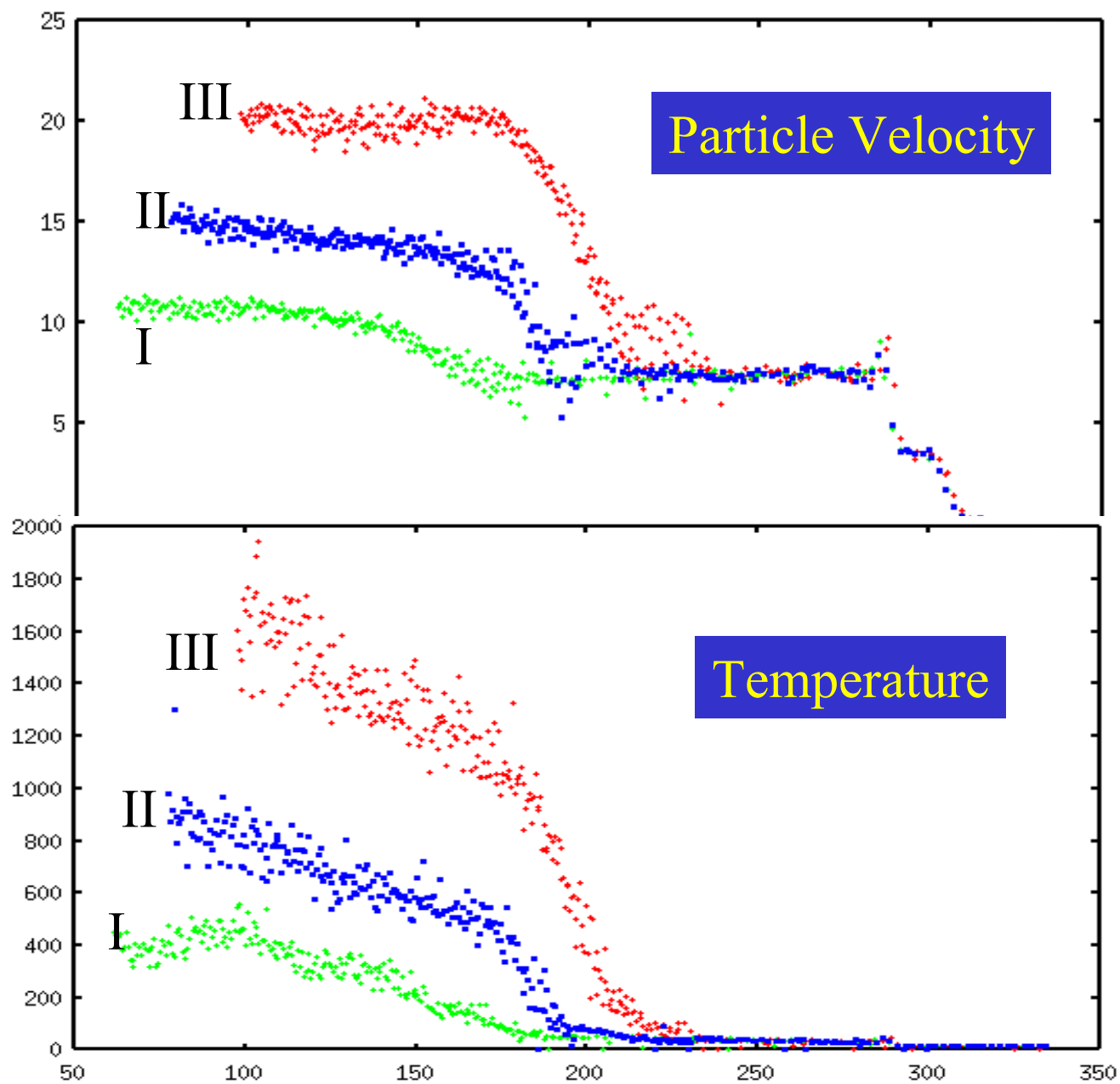
Shock Temperature:

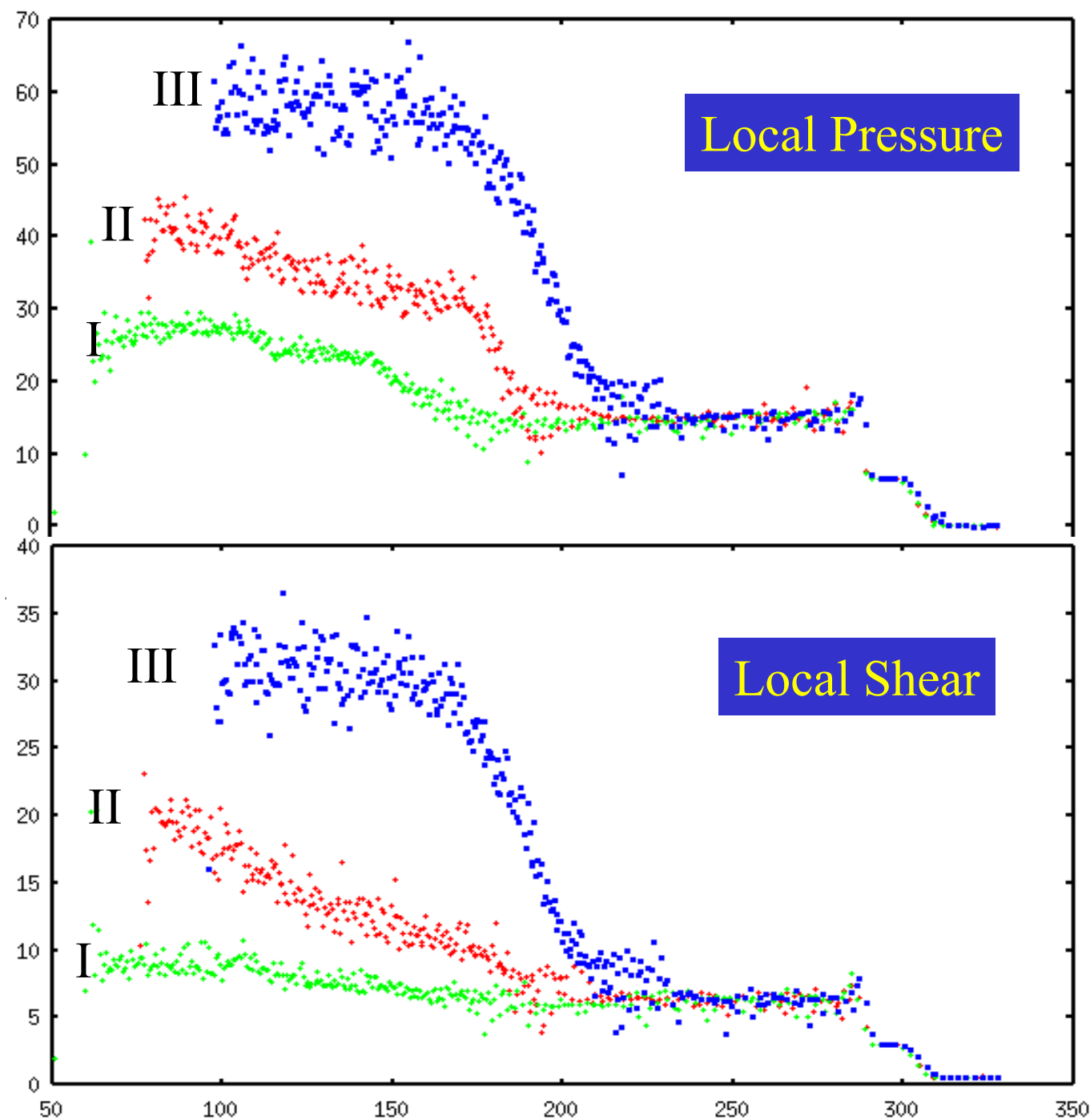
1800 K

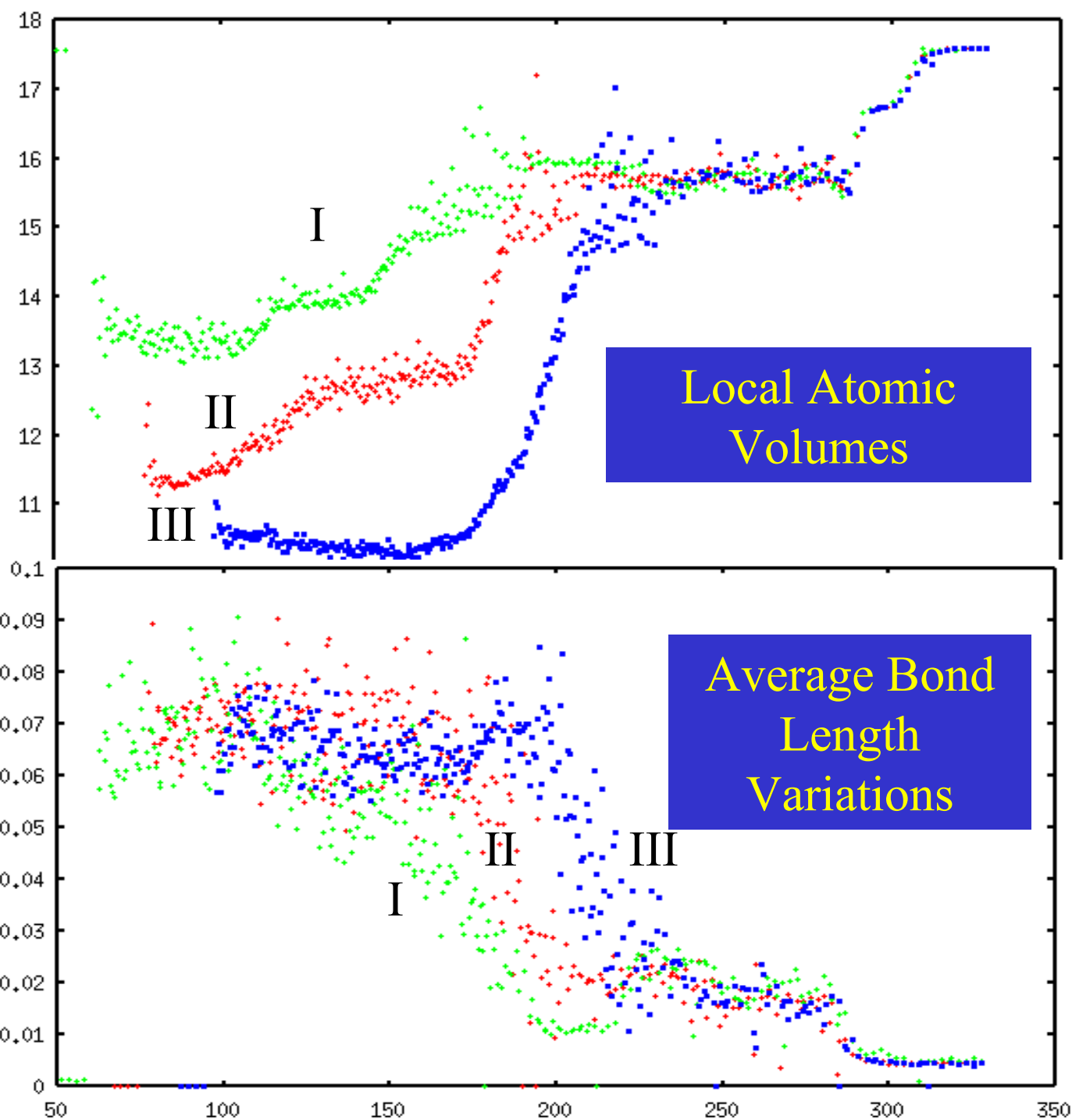
Shock Pressure:

60 GPa

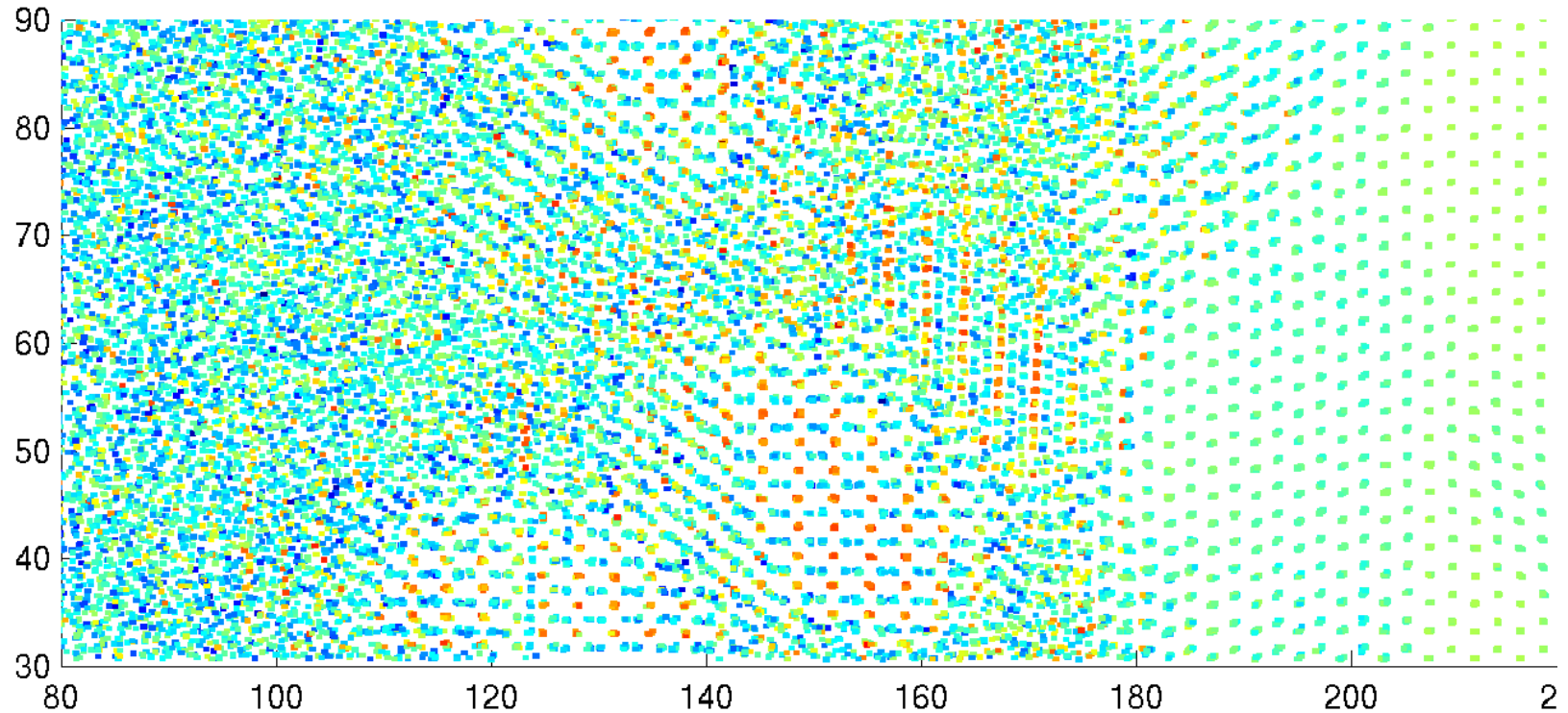




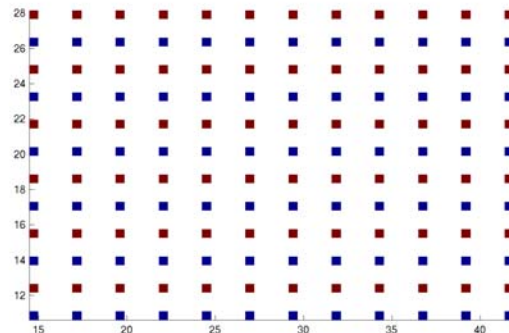




The yz-view of the whole sample



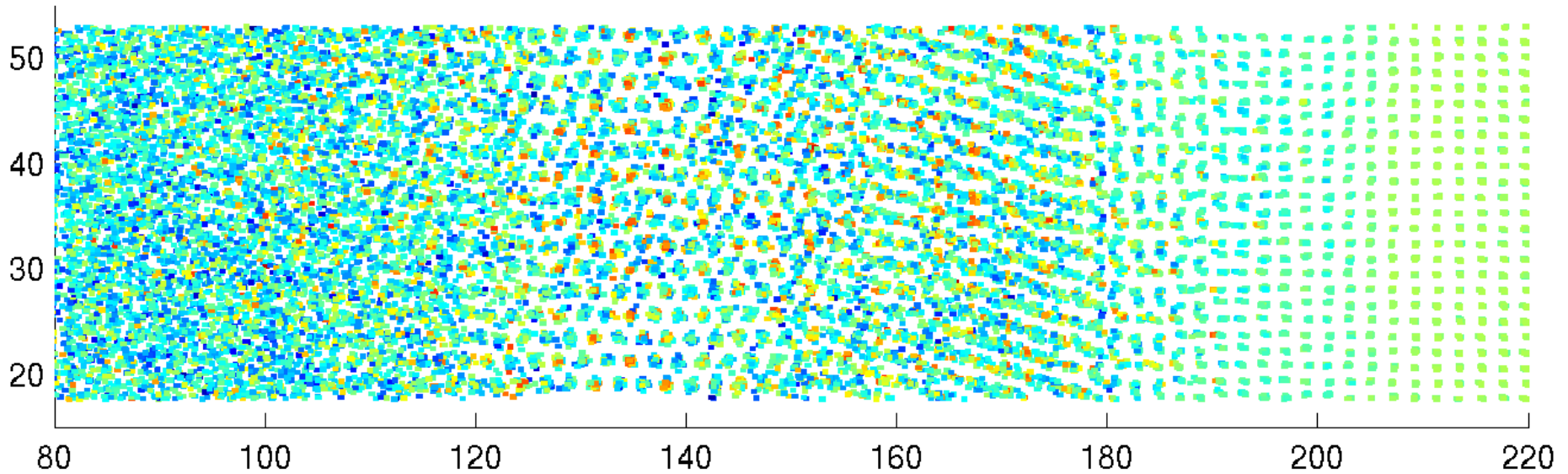
Omega phase



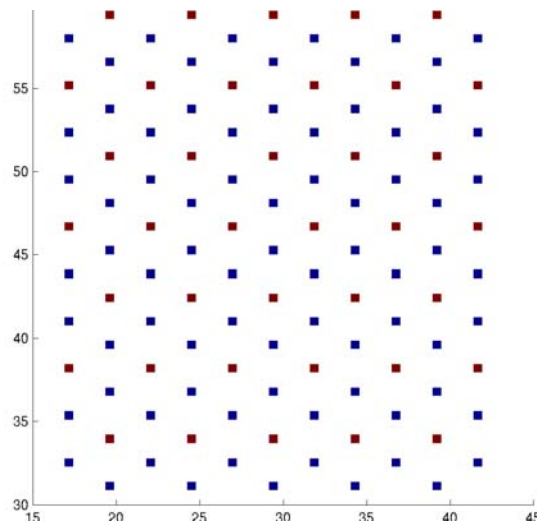
Coordination: 14

Coordination: 9

The xz-view of the whole sample



Omega phase



Coordination: 14



Coordination: 9